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RECEIVED 14 March 2025

ACCEPTED 10 April 2025

PUBLISHED 07 May 2025

CITATION

Yan Z, Jihong D, Yinglin L, Mengshan X and
Wen L (2025) Study on strength prediction of
grouting filling body in karst areas considering
pressure filter effect.
Front. Earth Sci. 13:1593528.
doi: 10.3389/feart.2025.1593528

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Study on strength prediction of grouting filling body in karst areas considering pressure filter effect

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The slurry within the grouting pressure and karst boundary constraints produces a pressure filtration effect, resulting in the initial consolidation strength of the embankment curtain stone body in karst areas being significantly higher than the natural consolidation strength of the slurry. Consequently, using the natural consolidation strength of the slurry as the initial condition for constructing the curtain life prediction model often leads to substantial deviations from engineering practice. To address this issue, this paper first derives a theoretical formula for calculating the initial consolidation strength of the grouted curtain body, taking into account the erosive effects of karst water ions and the pressure-filtering effect. Secondly, a life prediction model for grouting curtains in karst areas, which incorporates the pressure-filtering effect, is developed, and its feasibility is demonstrated through indoor accelerated testing. Finally, the research findings were successfully applied to guide the curtain de-reinforcement project at the Yingpan Reservoir in Yunnan Province. The results indicate that the theoretical formula for the initial consolidation strength of the grouted curtain body, which considers the pressure-filtering effect, more accurately characterizes the initial conditions of the curtain. Additionally, the theoretical values derived from the curtain life prediction model closely align with the accelerated experimental test values, with an error margin of less than 15%. This demonstrates that the theoretical prediction model can effectively forecast the service life of the curtain body under conditions of karst water erosion. The successful engineering application further confirms the feasibility and practicality of the theoretical prediction model. Given the increasing number of similar cases, the research findings hold significant application potential and practical value.

KEYWORDS

karst area embankment, pressure-filtration effect, grouted curtain body, strength calculation, life prediction

1 Introduction

In the 1950s–1970s, many dam projects were constructed in China. Due to the design standards, construction conditions, and level of mechanization at that time,

numerous dams experienced varying degrees of seepage, either during the initial stages of operation or after several years. This seepage significantly affected the operational safety of the dams (Ge et al., 2024; Jian et al., 2024; Xiang et al., 2022). Consequently, over the past decade, large-scale danger removal and reinforcement work has been conducted on dams in China. Grouting has played a crucial role in these projects due to its advantages, including simple construction, low environmental impact, and high construction efficiency (Fazeli, 2007; ZHANG et al., 2021; Dou et al., 2020). However, after a period of operation, some dams that underwent danger removal and reinforcement experienced seepage again, primarily in the areas of the grouting anti-seepage body. This issue is particularly pronounced in karst dams. Numerous studies have shown (Mozafari et al., 2021; Romanov et al., 2003) that the grouting anti-seepage body is susceptible to erosion and damage under the combined effects of high water pressure and karst water ions, leading to a significant reduction in its service life. Given the large number of dams in China and the widespread distribution of karst areas, researching the service life prediction of grouting curtains for dams in karst regions is of great practical significance and engineering value. This research can guide subsequent dam danger removal and reinforcement projects, as well as the design and construction of new dams.

At this stage, scholars have conducted extensive research on the life prediction of grouting curtains in karst areas through numerical simulation, model testing, and theoretical analysis, yielding significant results. In numerical simulations, Nagihara (1996), Wang et al. (2020), and others explored the deterioration of slurry crenellations in erosive environments by establishing a multivariate grey prediction model, a mechanical damage model for grouting plus solids under seepage, and a service life-cycle prediction model. Meanwhile, Dafny et al. (2015), Chen et al. (2022), and Huo et al. (2019) employed multi-coupled physical field software to investigate the decay processes and characteristics of service performance and impermeability in embankment curtains within karst areas. Although the numerical simulation results provide valuable insights for predicting the lifespan of grouted curtains in karst environments, these studies often simplify the karst water erosion process, leading to discrepancies between predicted lifespans and actual project outcomes. In terms of model testing, researchers have employed dry-and-wet cyclic deterioration tests (Muntaha, 2017; Zhou et al., 2022), accelerated erosion experiments (Paglia et al., 2003; Wang et al., 2021), drenching tests, and uniaxial compression tests (He et al., 2021; Ran et al., 2021) to investigate the performance deterioration of karst fillers, producing supportive findings for life prediction studies. However, due to limitations of model tests, it is challenging to conduct large-sample and long-cycle tests that comprehensively represent the entire service life of grouting curtains in karst areas. The theoretical analysis method, which can circumvent many shortcomings of model testing through specific assumptions and straightforward derivation processes, is increasingly being adopted by scholars for life prediction research on grouting curtains in karst areas. For instance, Dong et al. (2022) enhanced the initial weights and thresholds of a BP neural network using genetic algorithms to create a GA-BP model for predicting compressive strength; Peng (2012) developed a GA-BP model based on acid-base test methods to assess the service life of slurry-cemented bodies; and Hou et al. (2020) established a life-cycle

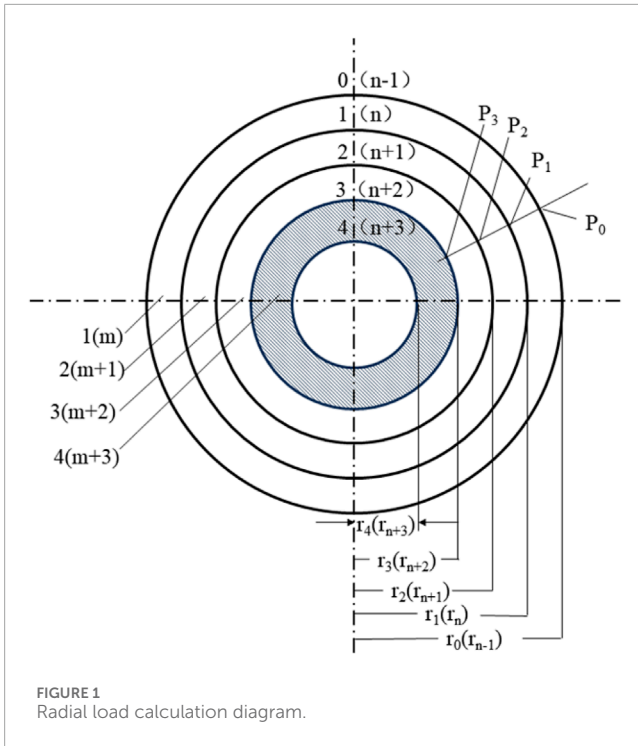
prediction model for slurry-cemented body specimens based on deformation modulus measurements from indoor tests. Literature reviews indicate that these studies advance theoretical research on life prediction for grouted curtains in embankment dams situated in karst areas. However, existing research often neglects the impact of the pressure-filtering effect on the performance of grouted curtains during formation, resulting in significant discrepancies between the initial conditions of life prediction models and engineering realities. Specifically, the slurry subjected to grouting pressure and constrained by karst boundaries produces a pressure-filtering effect (Chen et al., 2021), which precipitates free water and solidified water in the slurry. This results in the initial consolidation strength of the curtain stone body being significantly higher than that of the natural-state slurry consolidation strength (Axelsson et al., 2009; Eklund and Stille, 2008; Bouchelaghem et al., 2007). Therefore, using the natural consolidation strength of the slurry as the initial condition in life prediction models for curtains is unlikely to effectively guide engineering practice.

This paper first derives the theoretical formula for the initial consolidation strength of the grouting curtain body under karst water ion erosion, considering the filtering effect. Based on this theoretical formula, a life prediction model for the grouting curtain in karst areas is constructed. Next, the feasibility and practicality of the life prediction model are validated through indoor accelerated erosion tests of the cemented stone body, conducted using a self-developed filter-pressing grouting device. Finally, the grouting curtain life prediction model, which accounts for the pressure-filtering effect, is applied to the Zhumashao Reservoir in Kaiyuan City to determine the optimal grouting pressure during the design and construction stages of the reservoir. The results of this study aim to provide a reference for real-world projects.

2 Grouted curtain body life prediction model under pressure-filtration effect

2.1 Basic assumptions of the model

- (1) The slurry is an incompressible fluid, and its properties remain consistent throughout the diffusion process, adhering to Darcy's law.
- (2) The slurry undergoes cylindrical diffusion, resulting in a grout curtain body structure that is uniform, isotropic, and composed of incompressible homogeneous material.
- (3) During the filtration process, the structure and number of capillary pores within the grout curtain remain unchanged, allowing water in the slurry to precipitate freely.
- (4) The pressure-filtering effect is present throughout the entire grouting process; however, its influence varies along the horizontal direction of the grouting curtain.
- (5) The primary component of the cement slurry forming the curtain is calcium silicate, with hydrated calcium silicate gel playing a crucial role in determining the curtain's properties.
- (6) The hydration of cement in the grouting curtain is complete, and there is no air present in the pore spaces of the curtain.



2.2 Model construction and solution

Based on the above assumptions and references (Chen et al., 2021), it is evident that during the formation stage of the grout curtain, the cement slurry in the grouting process is influenced by a pressure-filtering effect. This effect causes the free and combined water in the slurry to continuously precipitate, resulting in the initial consolidation strength of the curtain body being significantly higher than the natural consolidation strength of the slurry. In the operational stage, the grout curtain body interacts with erosive ions present in the karst water. The calcium oxide within the grout curtain is gradually dissolved, which diminishes its seepage control and reinforcement capabilities until the grout curtain ultimately fails, marking the end of its service life. Therefore, during the formation stage of the grout curtain, and in accordance with assumptions (Equations 2–4), this paper performs a force analysis on a unit body within the curtain. The radial load calculation sketch is illustrated in Figure 1.

As shown in Figure 1, a cylindrical model of the curtain body is cut into rings of varying heights using a circular cross-section. Here, m denotes the number of rings, n denotes the number of demarcation surfaces, and r_n represents the radius of the rings. The radial pressure acting on the demarcation surface is P , the modulus of elasticity of the circular body is E , and the Poisson's ratio is μ . The equilibrium condition at the interface between the rings (Equation 1) is given by He (1990).

$$\begin{cases} U_{m,n} = U_{(m+1),n} \text{ (Equilibrium equation of radial displacement } U) \\ P_{m,n} = P_{(m+1),n} \text{ (Equilibrium equation of radial force } P) \end{cases} \quad (1)$$

If the height of the curtain is assumed to be h , the radial σ_r and tangential stresses σ_τ are related to the same radius by the equation.

$$\sigma_r = \frac{\frac{1-\mu}{Eh} \times \frac{r_1}{2} (r_2 - r_1) E}{1 - \mu} + \frac{\frac{1-\mu}{Eh} \times \frac{r_2}{2} (r_3 - r_2) E}{(1 + \mu)r^2} \quad (2)$$

$$\sigma_\tau = \frac{\frac{1-\mu}{Eh} \times \frac{r_1}{2} (r_2 - r_1) E}{1 - \mu} + \frac{\frac{1-\mu}{Eh} \times \frac{r_2}{2} (r_3 - r_2) E}{(1 + \mu)r^2} \quad (3)$$

The equilibrium differential equation for a planar circular ring under uniform external radial pressure is simplified as follows:

$$U = \sigma_1 r + \frac{\sigma_2}{r} \quad (4)$$

Two adjacent rings of circular cross-section, the m -th and the $(m+1)$ -th, are selected for analysis. The m -th ring is bounded by the radii r_{n-1} and r_n , and the $(m+1)$ -th ring is bounded by r_n and r_{n+1} . Then, the equilibrium differential equations of the planar circular rings under radial pressure for the m -th rings (Equations 5, 6) and $(m+1)$ -th rings (Equations 7, 8) are obtained from Equation 4 as:

$$\begin{cases} U_{m,(n+1)} = \frac{1-\mu}{Eh} \times \frac{r_{1,m}}{2} (r_{2,m} - r_{1,m}) r_{n+1} + \frac{\frac{1-\mu}{Eh} \times \frac{r_{2,m}}{2} (r_{3,m} - r_{2,m})}{r_{n+1}} \\ U_{m,n} = \frac{1-\mu}{Eh} \times \frac{r_{1,m}}{2} (r_{2,m} - r_{1,m}) r_n + \frac{\frac{1-\mu}{Eh} \times \frac{r_{2,m}}{2} (r_{3,m} - r_{2,m})}{r_n} \end{cases} \quad (5)$$

$$\begin{cases} \sigma_{r,m,(n+1)} = \frac{\frac{1-\mu}{Eh} \times \frac{r_{1,m}}{2} (r_{2,m} - r_{1,m}) E}{1 - \mu} - \frac{\frac{1-\mu}{Eh} \times \frac{r_{2,m}}{2} (r_{3,m} - r_{2,m}) E}{(1 + \mu)r_{n+1}^2} \\ \sigma_{r,m,n} = \frac{\frac{1-\mu}{Eh} \times \frac{r_{1,m}}{2} (r_{2,m} - r_{1,m}) E}{1 - \mu} - \frac{\frac{1-\mu}{Eh} \times \frac{r_{2,m}}{2} (r_{3,m} - r_{2,m}) E}{(1 + \mu)r_n^2} \end{cases} \quad (6)$$

$$\begin{cases} U_{(m+1),n} = \frac{1-\mu}{Eh} \times \frac{r_{1,m+1}}{2} (r_{2,m+1} - r_{1,m+1}) r_n + \frac{\frac{1-\mu}{Eh} \times \frac{r_{2,m+1}}{2} (r_{3,m} - r_{2,m+1})}{r_n} \\ U_{(m+1),(n+1)} = \frac{1-\mu}{Eh} \times \frac{r_{1,m+1}}{2} (r_{2,m+1} - r_{1,m+1}) r_{n+1} + \frac{\frac{1-\mu}{Eh} \times \frac{r_{2,m+1}}{2} (r_{3,m} - r_{2,m+1})}{r_{n+1}} \end{cases} \quad (7)$$

$$\begin{cases} \sigma_{\tau,(m+1),n} = \frac{\frac{1-\mu}{Eh} \times \frac{r_{1,m+1}}{2} (r_{2,m+1} - r_{1,m+1}) E}{1 - \mu} - \frac{\frac{1-\mu}{Eh} \times \frac{r_{2,m+1}}{2} (r_{3,m} - r_{2,m+1}) E}{(1 + \mu)r_n^2} \\ \sigma_{\tau,(m+1),(n+1)} = \frac{\frac{1-\mu}{Eh} \times \frac{r_{1,m+1}}{2} (r_{2,m+1} - r_{1,m+1}) E}{1 - \mu} - \frac{\frac{1-\mu}{Eh} \times \frac{r_{2,m+1}}{2} (r_{3,m} - r_{2,m+1}) E}{(1 + \mu)r_{n+1}^2} \end{cases} \quad (8)$$

When $U_{m,n} = U_{(m+1),n}$, then there were:

$$r_n (\sigma_{1,m} - \sigma_{1,m+1}) + \frac{1}{r_n} (\sigma_{2,m} - \sigma_{2,m+1}) = 0 \quad (9)$$

According to the system of Equation 6, the stress balance equations for m and $m+1$ neighboring rings can be obtained as

Equations 10, 11.

$$\begin{cases} \sigma_{1,m} = \frac{1-\mu}{E(r_{n-1}^2 - r_n^2)} \times \left(\frac{r_{n-1}^2 P_{n-1} - r_n^2 P_n}{h} \right) \\ \sigma_{2,m} = \frac{(1+\mu)r_{n-1}^2 r_n^2}{E(r_{n-1}^2 - r_n^2)} \times \frac{P_{n-1} - P_n}{h} \end{cases} \quad (10)$$

$$\begin{cases} \sigma_{1,(m+1)} = \frac{1-\mu}{E(r_n^2 - r_{n+1}^2)} \times \left(\frac{r_n^2 P_n - r_{n+1}^2 P_{n+1}}{h} \right) \\ \sigma_{2,(m+1)} = \frac{(1+\mu)r_n^2 r_{n+1}^2}{E(r_n^2 - r_{n+1}^2)} \times \left(\frac{P_n - P_{n+1}}{h} \right) \end{cases} \quad (11)$$

Bringing $\sigma_{1,m}$, $\sigma_{2,m}$, $\sigma_{1,(m+1)}$, $\sigma_{2,(m+1)}$ into Equation 9. The stress balance equations at the m and $m+1$ contact surfaces are shown in Equation 12.

$$l_m P_{n-1} - (l_m + l_m + 1 + b_n) P_n + l_m \cdot P_{n+1} = 0 \quad (12)$$

where P_{n-1} , P_n and P_{n+1} are the radial pressures acting on the ring at the separating interface (P_0 is the hydrostatic pressure, $P_0 = \rho gh$).

According to Reference He (1990), the expressions for the coefficients l_m , l_{m+1} and b_n are as follows:

$$l_m = \frac{r_{n-1}^2 r_n^2}{Eh(r_{n-1}^2 - r_n^2)} \quad (13)$$

$$l_{m+1} = \frac{r_n^2 r_{n+1}^2}{Eh(r_n^2 - r_{n+1}^2)} \quad (14)$$

$$b_n = \frac{r_n^2}{2} \times \frac{1-\mu}{Eh} \quad (15)$$

Expression of coefficients in Equations 13–15, where r_{n-1} , r and r_{n+1} are the radii of the interfaces when the number of interfaces is n .

According to the assumption condition (Equation 2), the trinomial system of equations is obtained as follows:

$$\begin{cases} P_0 - (l_1 + l_2 + \sigma_1)P_1 + l_2 P_2 = 0 \\ P_1 - (l_2 + l_3 + \sigma_2)P_2 + l_3 P_3 = 0 \\ l_3 P_2 - (l_3 + l_4 + \sigma_2)P_3 = 0 \\ l_n = \frac{r_{n-1}^2 r_n^2}{Eh(r_{n-1}^2 - r_n^2)} \end{cases} \quad (16)$$

Substitute $l_1, l_2, l_3, l_4, \sigma_1, \sigma_2, \sigma_3$ into Equation 16 to find the pressure P at the contact surface of the ring as follows:

$$\begin{cases} P_1 = \frac{(a_2 a_3 - l_3^2) l_1}{a_1 a_2 a_3 - (a_1 l_3^2 + l_2^2 a_3)} \cdot P_0 \\ P_2 = \frac{l_1 l_2 a_3}{a_1 a_2 a_3 - (a_1 l_3^2 + l_2^2 a_3)} \cdot P_0 \\ P_3 = \frac{l_1 l_2 l_3}{a_1 a_2 a_3 - (a_1 l_3^2 + l_2^2 a_3)} \cdot P_0 \\ a_1 = l_1 + l_2 + O_1 \\ a_2 = l_2 + l_3 + O_2 \\ a_3 = l_3 + l_4 + O_3 \end{cases} \quad (17)$$

Take the average value of P_1 , P_2 , and P_3 as the natural consolidation strength f_0 of the grouted curtain body. Then,

$$f_0 = \frac{P_1 + P_2 + P_3}{3} \quad (18)$$

According to the assumption condition (Equation 5) and in combination with the research findings of POWERS (1960), Equation relationship between the initial consolidation strength f of the grouted curtain body considering the pressure-filtering effect and the gel-void ratio X of the curtain body:

$$f = f_0 \cdot X^n \quad (19)$$

where X is the gel-void ratio; n is an experimental constant ranging from 2.6 to 3.0, which is related to the type of cement and experimental conditions.

According to Reference (Chen et al., 2021), the calculation formula for the gel-void ratio is as follows:

$$X = \frac{V_p}{V_s} \quad (20)$$

$$V_p = V_s + V_d + V_h \quad (21)$$

where V_p represents the pore volume of the curtain body filling the fractures after drainage and hydration under the grouting pressure (m^3); V_s is the volume of the grout curtain body, which is also the volume of the grout filling the fractures (m^3); V_d is the volume of the drained water from the grout filling the fractures during the grouting project (m^3); V_h is the volume of the hydration water in the grout (m^3).

The volume V_s of the grout curtain body can be calculated by Equation 22:

$$V_s = \pi r^2 h \quad (22)$$

During a variable time interval dt in the grouting process, the reduction in the pore volume within the unit body should be equal to the amount of water seeped out, that is Equation 23:

$$\frac{\partial V_s}{\partial t} dt = \frac{\partial q}{\partial h} dh dt \quad (23)$$

where t is the time (s); q is the amount of water seeped out from the pores (m^3). Generally, the pore diameter of the cement curtain body ranges from 10^{-5} to 10^{-10} m. Based on the assumption condition (Equation 3), it can be deduced that:

$$q = \frac{pr^4}{gh} J \quad (24)$$

where r is the radius of the pore (m), which gradually decreases as the pore water is discharged; J is the hydraulic gradient in the pore ($MPa \cdot m^{-1}$); η is the viscosity coefficient of water (Pa·s).

After the grouting time t , the total amount of water seeped out from the pores is:

$$V_d = \int \frac{\pi r^4}{g\eta} J t N dt \quad (25)$$

where N is the number of pores on the calculation cross-section.

According to Reference Chen et al. (2021), the amount of water required for the hydration reaction with cement particles during complete hydration is 0.227 times the mass of the cement particles. Therefore, the formula for calculating the volume V_h of hydration water in the Equation 26:

$$V_h = 0.227 \times \frac{V_s \rho_s m_c}{1 + (m_w/m_c) \rho_w} \quad (26)$$

where ρ_s is the density of the grout ($\text{kg}\cdot\text{cm}^{-3}$); ρ_w is the density of water ($\text{kg}\cdot\text{cm}^{-3}$); m_c and m_w are the masses of cement particles and water in a unit volume of the grout (kg), respectively.

Therefore, according to the different durations of pressure application during the grouting process, the initial consolidation strength f of the curtain body considering the pressure-filtration effect can be obtained as follows:

$$f = f_0 \times \left[\frac{\pi r^2 h + \int \frac{\pi r^A}{g\eta} t N dt + 0.227 \times \frac{\pi r^2 h \rho_s m_c}{1+(m_w/m_c)\rho_w}}{\pi r^2 h} \right]^n \quad (27)$$

During the operational stage of the grouted curtain body, ion erosion from karst water causes continuous dissolution of calcium oxide within the grouting material. As calcium oxide dissolves, solid-phase calcium hydroxide begins to dissolve as well. Subsequently, high-alkaline hydrated silicates and hydrated aluminates decompose into low-alkaline hydrates, ultimately transforming into substances such as gaseous silicon dioxide, which lacks cementing ability (Gao et al., 2024). Additionally, the consumption rate of calcium oxide is closely related to the pH of the environment (Peng, 2012). Consequently, the degree of strength attenuation in the curtain body varies with different pH levels.

The standard curve of the strength-pH of the calcified body is fitted using the plotting software SPSS (Version 19.0), and the Equation 28 of the standard curve is obtained.

$$F = f + \frac{A}{w\sqrt{\frac{\pi}{2}}} e^{-2\frac{(pH-pH_0)^2}{w_1^2}} \quad (28)$$

where F is the residual strength of the curtain body after being eroded by karst water; f is the initial consolidation strength; pH_0 is the initial pH of the solution; A and w_1 are constants obtained from the curve fitting.

Based on the unconfined compressive strength of the calcified body obtained from the experimental tests, a relationship curve between the strength and the service life of the calcified body is plotted. Then, the plotting software is used to fit the standard curve of the strength-service life of the calcified body, and the calculation formula of the standard curve is obtained as follows:

$$F = f + B e^{\frac{(t-T_c)^2}{2w_2^2}} \quad (29)$$

where T_c is the initial time constant of the solution; B and w_2 are constants obtained from the curve fitting.

According to Reference Peng (2012), the strength of the grouting curtain body and the pH of the karst water satisfy the following relationship:

$$pH = pH_0 + \zeta(R) \quad (30)$$

where R is the attenuation rate of the compressive strength.

Combining Equations 18, 27, 30, we can obtain the residual strength of the curtain body's initial consolidation strength after erosion by karst water:

$$F = \frac{P_1 + P_2 + P_3}{3} \cdot \left(\frac{\pi r^2 h - \int \frac{\pi r^A}{g\eta} t N dt - 0.227 \times \frac{\pi r^2 h \rho_s m_c}{1+(m_w/m_c)\rho_w}}{\pi r^2 h} \right)^n \cdot R \quad (31)$$

Taking the reaction between hydrochloric acid and cement stone as an example, m moles of $\text{Ca}(\text{OH})_2$ will consume $2m$ moles of hydrochloric acid. When the volume of the corrosive solution is n liters and the initial pH is pH_0 , the consumption of $\text{Ca}(\text{OH})_2$ and the pH of the solution satisfy the following relationship:

$$pH = \lg \left(\frac{n}{n10^{-pH_0} - 2m} \right) \quad (32)$$

where n is the volume of the corrosive solution; m is the cumulative consumption of CaO ; pH_0 is the initial pH of the corrosive solution.

Combining Equation 30 and Equation 31 and substituting the critical pH_T calculated from Equation 32 into the combined formulas, the service life T of the grouted calcified body can be calculated.

Numerous studies have shown (Huo et al., 2019; Peng, 2012) that the consumption rate of calcium oxide in the grouted curtain body (i.e., the ratio of the consumed amount to the original internal total amount) is closely related to the strength of the grouted curtain body. Especially when the cumulative consumption rate of calcium oxide exceeds 25%, the strength of the curtain body will decline sharply, indicating that the grouted curtain has failed. Therefore, the failure of the curtain body, defined as reaching the critical value of its service life, occurs when its initial consolidation strength diminishes to 50% in a karst water environment.

There is the following relationship between the compressive strength of the curtain body and its service life:

$$R = \eta(t) \quad (33)$$

where R is the attenuation rate of the compressive strength decay rate versus erosion time equation.

Therefore, by combining Equations 28–31, the service-life prediction model for the grouted curtain in karst areas considering the pressure-filtration effect can be obtained as follows:

$$\begin{cases} f = \frac{P_1 + P_2 + P_3}{3} \cdot \left(\frac{V_p}{V_s} \right)^n \cdot R \\ pH - pH_0 = \zeta(R), \quad pH = \lg \left(\frac{n}{n10^{-pH_0} - 2m} \right) \\ R = \eta(t), \quad T = t | \text{CaO} = 25\% \end{cases} \quad (34)$$

2.3 Determination of model formula parameters

- (1) In the formula, the elastic modulus E and Poisson's ratio μ of the grouting curtain body can be obtained through tests using a triaxial stress testing machine. Specifically, the specifications in the Standard for Geotechnical Test Methods (Ministry of Water Resources of the People's Republic of China, 2019) should be referred to.
- (2) The hydraulic gradient ($\text{MPa}\cdot\text{m}^{-1}$) in the pores is equal to the ratio of the water head difference p to the drainage length h . The calculation can be seen in Equation 35:

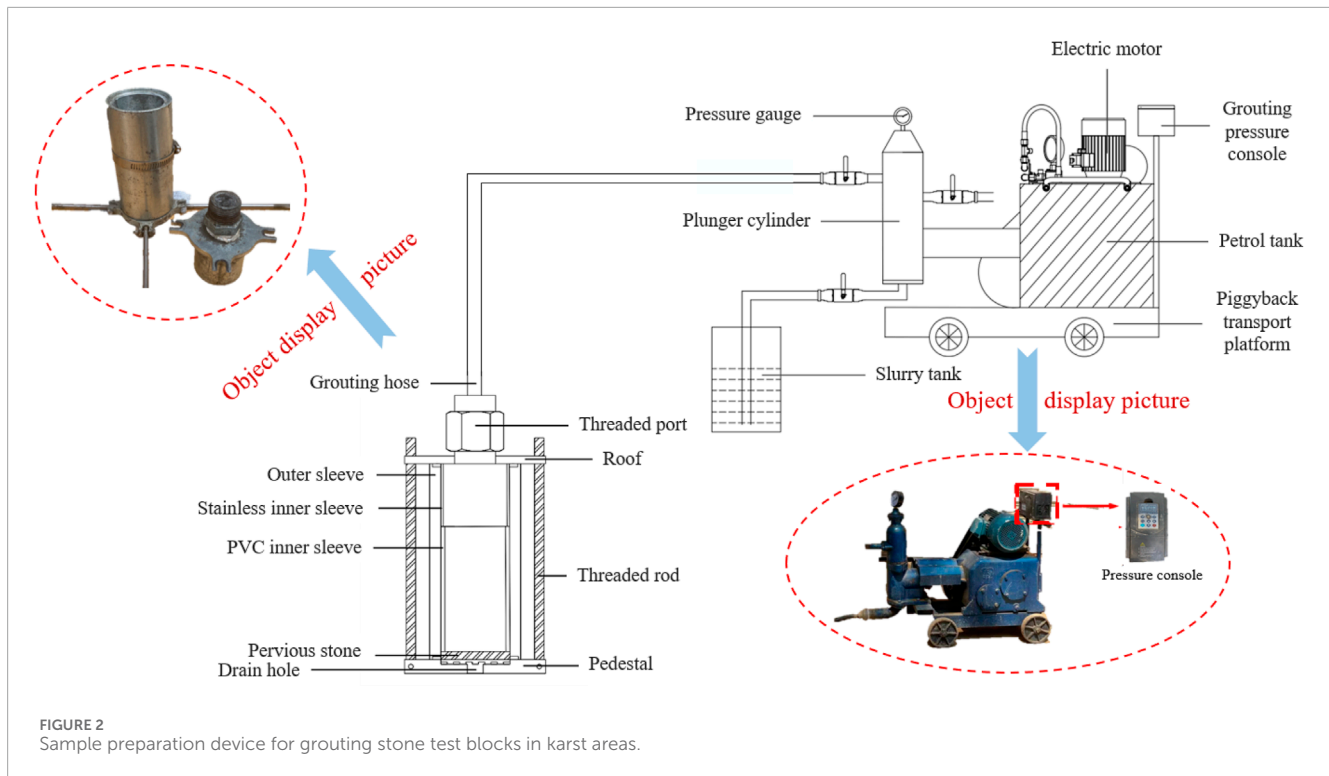


FIGURE 2
Sample preparation device for grouting stone test blocks in karst areas.

$$J = \frac{p}{h} \quad (35)$$

- (3) The η is defined as the viscosity coefficient of water at 20°C, which is generally taken as 1.0087.
- (4) The density of the grout ρ_s is equal to the ratio of the average saturated mass in the initial state to the volume of the specimen. The density of water ρ_w is generally taken as $1 \times 10^3 \text{ kg}\cdot\text{m}^{-3}$.
- (5) The N -values of grouts with different water-cement ratios can be calculated by referring to the test method in Reference You (2010).

3 Verification of the service - life prediction model

3.1 Pressure-filtration sample preparation system

To verify the feasibility of the derived service-life prediction model for the grouting curtain under the pressure filtration effect, a set of sample preparation equipment was developed for creating grouting test blocks of calcified bodies in karst areas, as shown in Figure 2. This equipment comprises two main components: a constant-pressure grouting machine and a sample preparation mold. By utilizing the properties of filter paper and permeable stones, which permit water to pass through while preventing grout from doing so, specimens of

grouting-reinforced bodies can be created using different grouting materials and construction parameters under the pressure-filtration effect.

3.2 Specimen preparation and curing

3.2.1 Specimen preparation

In this test, pure cement grout was selected to create specimens of the grouting calcified body. The grout was prepared according to the commonly used mix proportions for grouting curtains in karst areas. Specifically, the water-to-cement ratio of the pure cement grout was 1:2, the grouting pressure was set at 1 MPa, and the grouting time was 6 s.

3.2.2 Specimen curing

Curing was conducted in accordance with the standard requirements outlined in the Standard for Test Methods of Mechanical Properties of Ordinary Concrete (Ministry of Construction of the People's Republic of China, 2019). These standards specify a temperature of $20^\circ\text{C} \pm 1^\circ\text{C}$ and a humidity level of at least 95%.

3.3 Design of accelerated deterioration of specimens

To determine the service life of the grouting curtain body in a karst water environment within a short time frame, this paper accelerates the deterioration process of the grouting calcified body by adjusting the concentration of corrosive

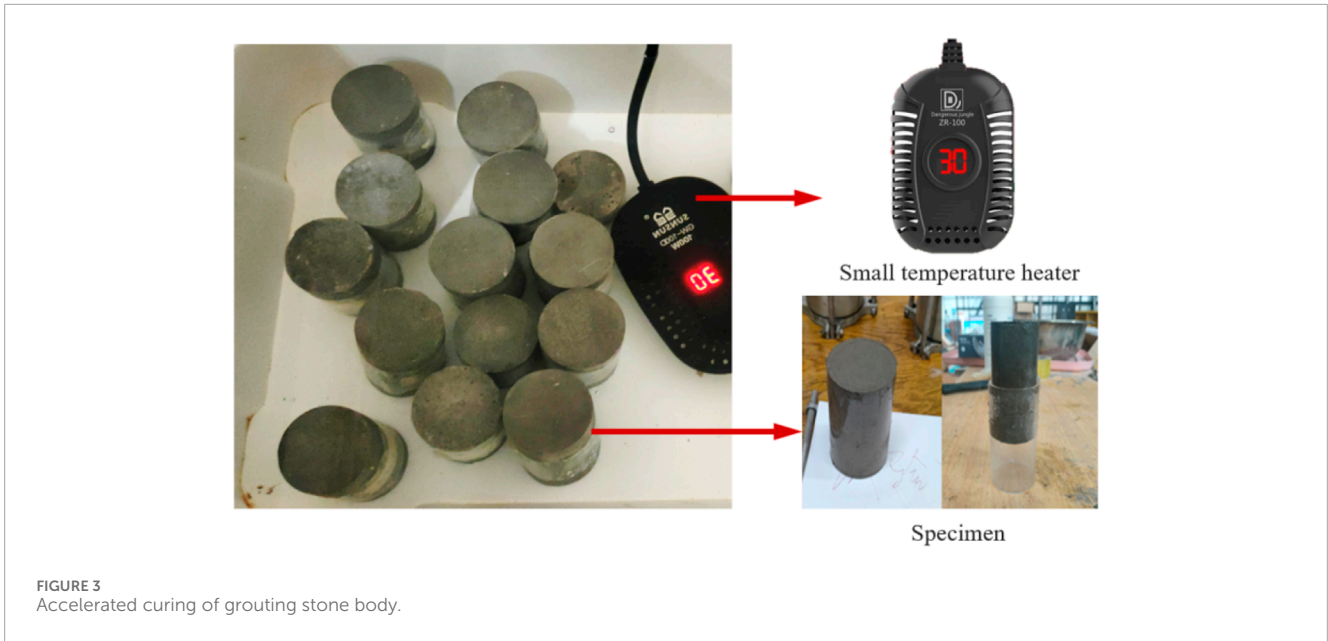


FIGURE 3 Accelerated curing of grouting stone body.

ions in the karst water and the curing temperature. The accelerated deterioration curing of the specimens is illustrated in Figure 3.

3.3.1 Acceleration by ion concentration

When the influence of the binding capacity of aggressive ions within the grouted stone body and the time-dependent structural defects on the diffusion coefficient is not considered, the diffusion theoretical model of aggressive ions (Equation 36) can be obtained based on Fick's second law (Zuo et al., 2012):

$$c = c_s \left(1 - \operatorname{erf} \frac{x}{2\sqrt{Dt}} \right) \quad (36)$$

where c_s is the concentration of aggressive ions on the exposed surface of the grouted stone body ($\text{mol}\cdot\text{L}^{-1}$); erf is the error function, $\operatorname{erf}_u = \frac{2}{\pi} \int_0^u e^{-t^2} dt$.

If the concentration c_s of aggressive ions on the exposed surface of the grouted stone body is increased by 20 times, then the test acceleration factor $s_1 = 20$.

3.3.2 Temperature acceleration

In the test, the grouting reinforced body test blocks are cured at a constant temperature of 30°C. Then, according to the influence of the environmental temperature on the diffusion of aggressive ions in the calcified body in the Arrhenius equation, the acceleration coefficient s_2 can be calculated as shown in Equation 37:

$$s_2 = \frac{D_T(303)}{D_T(290.9)} = \frac{D_0 e^{\frac{E}{R} \left(\frac{1}{293} - \frac{1}{303} \right)}}{D_0 e^{\frac{E}{R} \left(\frac{1}{291} - \frac{1}{293} \right)}} = 6.95 \quad (37)$$

where D_0 is the diffusion coefficient of aggressive ions at temperature T_0 ($\text{m}^2\cdot\text{s}^{-1}$); D_T is the diffusion coefficient of aggressive ions at temperature T ($\text{m}^2\cdot\text{s}^{-1}$); T_1 is the reference temperature, generally taken as 293K; E/R is the activation energy, which is taken as 14,242 according to the test values in Atkinson.

Therefore, the total acceleration factor S of this deterioration test is equal to the product of the acceleration factor of the external aggressive ion concentration and that of the temperature, that is, $S = 138.94$.

3.4 Test results and comparative analysis

In the laboratory test, the values of the model parameters are as follows: the elastic modulus $E = 20$ GPa; Poisson's ratio $\mu = 0.2$; the test constant n is taken as 3.0; the hydraulic gradient $J = 12.5$ MPa; the viscosity coefficient $\eta = 1.0087$; the number of pores on the cross-section $N = 2$; the density of the grout $\rho = 1.745 \times 10^3$ $\text{kg}\cdot\text{m}^{-3}$. Given that the water-cement ratio of the pure cement grout is 1:2, the volume of cement particles $V_c = 0.33$ m^3 and the volume of water $V_w = 0.67$ m^3 in a unit volume of the grout can be obtained. The volume of the corrosion solution $n = 0.1$ m^3 , and the initial pH value of the corrosion solution $\text{pH}_0 = 5.5$. The grouted stone specimens cured in the karst water environment for different durations were subjected to unconfined compression tests, and the results were compared with those of the theoretical model. The test results and the theoretical calculation results are presented in Table 1.

As shown in Table 1, the predicted values from the theoretical model are relatively close to the actual values obtained from experimental tests, with variances all less than 0.35. This indicates that the prediction model has good accuracy. During the accelerated erosion test, the calcified body reaches its service life after approximately 150 days of exposure to karst water curing. Using the acceleration factor of 138.94 applied in the accelerated test, we estimate its service life in a karst environment to be about 57 years. The theoretical predicted value is 63 years, with an error margin of less than 15%. This suggests that the prediction model can effectively guide engineering practice.

TABLE 1 Calculated compressive strength values of grouting stone body.

Time	Test value of compressive strength (MPa)	Calculated value of compressive strength (MPa)	Variance
Initial state	35.92	36.49	0.081
Karst water 30d	30.70	31.78	0.292
Karst water 60d	27.49	26.48	0.255
Karst water 90d	25.88	26.72	0.176
Karst water 120d	21.42	21.97	0.076
Karst water 150d	18.10	18.74	0.102



FIGURE 4
Construction photos of the site.

4 Application in a typical engineering project

4.1 Project background

The Zhumashao Reservoir is a small-sized (Type II) water conservancy project primarily intended for agricultural irrigation. It features a homogeneous earth dam with a maximum height of 9.0 m, a crest length of 110.3 m, a crest width of 3.6 m, and a crest elevation of 1359.00 m. The total storage capacity is 185,600 m³. This dam site is situated in a karst depression, where the main unfavorable geological phenomenon is karst formation. Karst caves and fissures are well-developed in the area, with cave cavities often filled with clay. The dam was initially constructed in February 1970 and completed for water storage in July 1971. Due to the dam-building technology and economic conditions at that time, certain potential safety hazards were present in the project. As a result, multiple rounds of hazard removal and reinforcement work were carried out subsequently. However, after several years of operation,

issues such as seepage in the dam body and at the contact zone between the dam body and the foundation, as well as seepage in the reservoir area caused by the karst-developed zone near the reservoir bank, persisted.

4.2 Construction scheme and effect evaluation

Curtain grouting was implemented to eliminate potential hazards and reinforce the dam. The bottom boundary of the anti-seepage curtain grouting treatment was controlled based on a permeability rate of $q \leq 10$ Lu. The axis of the curtain grouting aligned with that of the dam, and the depth of the curtain extended 5 m below the bottom boundary of the dam body. The grouting curtain consisted of single-row holes spaced 1.5 m apart, with hole depths ranging from 3.5 m to 13.97 m. The grouting material used for the dam body was a cement-clay slurry, employing conventional grouting techniques, while the dam foundation was grouted with

pure cement slurry. The anti-seepage standards for curtain grouting stipulated that the permeability coefficient of the dam body should be $k \leq 10^{-5}$ cm/s, and the permeability rate of the bedrock should be $q \leq 10$ Lu. The total length of the anti-seepage line for the curtain grouting was 118.26 m. A total of 77 production holes were drilled, resulting in a total drilling footage of 890.33 m and a total grouting section length of 752.35 m. Given that the expected service life of a small-sized water conservancy dam is approximately 100 years ($t = 100$ a), substituting this value into Equation 34 yields a final grouting pressure of 0.3 MPa necessary to meet the service-life requirement. The on-site construction process is depicted in Figure 4.

During the construction process, the treatment measures implemented were both reasonable and effective. Following the completion of the anti-seepage project, the anti-seepage effect was remarkable, as confirmed by the water pressure test conducted on the inspection holes. The trial water storage of the reservoir showed normal water balance analysis, indicating that the project's anti-seepage measures met the expected goals.

5 Conclusion

- (1) Based on the deterioration law of the initial consolidation strength of the curtain body under karst erosion conditions, a service-life prediction model for the grouting curtain of dams in karst areas considering the filter-pressing effect has been established. This model is simple to calculate, and its parameters are easy to obtain. It can efficiently and accurately predict the service life of grouting curtains in karst areas, demonstrating good practicality and applicability. Furthermore, this model can not only guide the design and construction of grouting curtains for dams in karst areas, but it can also be applied to similar projects in these regions, providing a new approach for predicting the service life of grouting curtains in karst areas.
- (2) An accelerated erosion test of the grouting curtain calcified body in a karst environment, under the filter-pressing effect, was conducted. This study explored the strength deterioration of the grouting curtain calcified body and verified the feasibility of a theoretical model for predicting its service life. With a water-cement ratio of 1:2 for the pure cement grout, a grouting pressure of 1 MPa, and a grouting time of 6 s, the measured service life of the calcified body was 57 years, while the theoretical predicted value was 63 years, resulting in an error of less than 15%. This indicates that the prediction model can effectively guide engineering practice.
- (3) A sample-making device for dams in karst areas, which considers the filter-pressing effect, has been independently designed and developed. This device can produce standard calcified body specimens under various grouting parameters for compressive strength testing. It is easy to operate and boasts high sample-making efficiency, providing new equipment for testing the performance of grouting materials in karst environments. Additionally, by adjusting the mesh numbers of the filter paper and the permeable stone, calcified body specimens with different filter-pressing coefficients can be obtained for performance testing.
- (4) The research results have been successfully applied to guide the curtain danger removal and reinforcement project of the Yingpan Reservoir in Yunnan Province, further demonstrating the feasibility and practicality of the theoretical prediction model. Based on the on-site investigation data from Yingpan Reservoir and aligned with the service life requirements stipulated in the design, the construction parameter for the curtain danger removal and reinforcement were determined using the research findings from this paper. The subsequent evaluation of the grouting effect achieved the expected goals. Given the practicality and applicability of the curtain body service life prediction model developed in this paper, this method can be further promoted and applied in the design and construction of grouting curtains in the fields of transportation, mining, and industrial and civil construction in karst areas.
- (5) A sample-making device for dams in karst areas considering the filter-pressing effect was independently designed and developed. It can obtain standard calcified body specimens under different grouting parameters for compressive strength testing. This device is easy to operate and has high sample - making efficiency, providing a new piece of equipment for testing the performance of grouting materials in a karst environment. In addition, by adjusting the mesh numbers of the filter paper and the permeable stone, grouting calcified body specimens with different filter-pressing coefficients can be obtained for performance testing.
- (6) The research results have been successfully applied to guide the curtain danger - removal and reinforcement project of Yingpan Reservoir in Yunnan Province, further demonstrating the feasibility and practicality of the theoretical prediction model. Based on the on-site investigation data of Yingpan Reservoir and combined with the service-life requirements stipulated in the design, the construction parameter control conditions such as the grouting material mix ratio and the designed grouting pressure value (> 0.3 MPa) for the curtain danger-removal and reinforcement were determined using the research results of this paper, and the subsequent evaluation of the grouting effect achieved the expected goals. Considering the practicality and applicability of the curtain body service-life prediction model derived in this paper, this method can be further popularized and applied in the design and construction of grouting curtains in the fields of transportation, mining, industrial and civil construction in karst areas.

Data availability statement

The raw data supporting the conclusions of this article will be made available by the authors, without undue reservation.

Author contributions

ZY: Writing – original draft, Data curation, Validation, Writing – review and editing. DJ: Methodology, Writing – review and editing, Conceptualization. LY: Conceptualization, Writing – review and editing. XM: Writing – original draft, Methodology. LW: Data curation, Writing – review and editing.

Funding

The author(s) declare that financial support was received for the research and/or publication of this article. This work was supported by the Major water conservancy science and technology project of Hunan Province (XSKJ2023059-02) and the water conservancy science and technology project of Yunnan Province (Project Name: Research on Key Technologies of Intelligent Grouting in Soft Strata and System Integration). The corresponding author gratefully acknowledges this financial support.

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